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INDENTATION LAW FOR COMPOSITE LAMINATES

by

S.H. Yang and C.T. Sun

July 31, 1981

COMPOSITE MATERIALS LABORATORY

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NOMENCLATURE

D_S	Diameter of the spherical indentor
E ₁	Longitudinal modulus of elasticity
E ₂	Transverse modulus of elasticity
ES	Young's modulus for sphere
E _t	Young's modulus for target
F	Contact force
$F_{\rm m}$	Maximum contact force at unloading
G ₁₂	In-plane shear modulus of elasticity
R_{S}	Radius of sphere
k	Contact coefficient
k ₁	Reloading coefficient
k'	Contact coefficient with the unit of stress
S	Unloading coefficient
α	Indentation
^α o	Permanent indentation
αcr	Critical indentation
α m	Maximum identation at unloading
ν _S ·····	Poisson's ratio of sphere
νt	Poisson's ratio of target

1. Introduction

It is well recognized that composite laminates are susceptible to damage resulting from impact of foreign objects. In general, hard and soft objects result in different failure modes. If the object is relatively rigid and small, then the contact time is short and extensive damage occurs in the neighborhood of the contact region. The extent of damage obviously depends on the contact force between the object and the target composite. An accurate account of the contact force and indentation is necessary to quantify the impact damage.

Direct measurement of the dynamic contact force is not an easy task due to the wide range of impact velocities and other parameters, and limitations of experimental techniques. The objective of this study is to determine experimentally static indentation laws for epoxy-based composite laminates in contact with steel balls and then model them in power laws.

The most famous elastic contact law, $F = k\alpha^{3/2}$, was derived by Hertz [1] for the contact of two spheres of elastic isotropic materials based upon theory of elasticity. The contact between a sphere and a half-space is a limiting case. Since this contact law is derived based upon the contact of elastic spheres, one faces several uncertainties when applying it to laminated composites. First, most laminated composites in use can not be adequately represented by a half-space. Second, the anisotropic and nonhomogeneous property of laminated composites may alter the form of the law. Third, the strain rate which is not accounted for by the Hertzian law may have significant effects on the $F - \alpha$ relation.

Except for the strain rate effect, the first two uncertainties may be

cleared by analyzing the exact contact problem of a sphere pressed into a laminated composite by using three-dimensional elasticity. However, experience tells us that analytical solutions for such contact problems are extremely difficult to obtain especially if permanent deformations are to be accounted for during unloading. Since unloading paths are important as far as the local damage zone is concerned, in this study, an experimental approach is taken to determine the law of contact for composites. However, the strain rate effect is neglected.

2. Hertzian Law of Contact

When two solid bodies are in contact, deformation takes place in the contact zone and the contact force results. Once the contact force is obtained, conventional methods for stress analysis can be used to find the stress distribution in the bodies. Determination of the contact force-indentation relationship often becomes the most important step in analyzing the contact problem.

A special case of the Hertz contact problem is the contact of an elastic sphere and an elastic half space. The contact force F and the indentation depth α have the relation

$$F = k \alpha^{3/2} \tag{1}$$

where

$$k = (4/3) (R_s)^{1/2} [(1 - v_s^2)/E_s + (1 - v_t^2)/E_t]^{-1}$$
 (2)

In equation (2), R_S is the radius of the sphere, ν is the Poisson's ratio, E is the Young's modulus, and subscripts s and t indicate the sphere and the target, respectively. Equation (1) is usually called the Hertzian law of contact for a sphere in contact with a half-space.

The 1.5 power given by equation (1) was found to be valid by Willis [2] for a rigid sphere pressed on a transversely isotropic half-space. A modified contact law with

$$k = (4/3) (R_s)^{1/2} [(1-v_s^2)/E_s + 1/E_2]^{-1}$$
 (3)

was employed by Sun [3] for a study on impact of laminated composites. In equation (3), R_s , v_s and E_s are the radius, the Poisson's ratio and the Young's modulus of the isotropic sphere, respectively, and E_2 is the modulus of elasticity transverse to the fiber-direction in the fiber-reinforced composite.

A more general form for the contact law was proposed by Meyer [4] as

$$F = k \alpha^{n}$$
 (4)

which has been found suitable for many static indentations. It is obvious that when n = 1.5 and k given by equation (2) this relation reduces to the Hertzian law for isotropic bodies.

Permanent indentation in composite targets often takes place even at relatively low loading levels. Thus, the aforementioned indentation laws for elastic bodies are valid only for the loading process. To account for the permanent deformation, the following power law was suggested by Crook [5].

$$F = F_{m} [(\alpha - \alpha_{o})/(\alpha_{m} - \alpha_{o})]^{q}$$
(5)

where F_m is the maximum contact force just before unloading, α_m is the indentation corresponding to F_m , and α_0 is the permanent indentation during this loading-unloading cycle. This unloading law was used by Barnhart and Goldsmith [6] for impact of a steel ball onto an armor plate.

Experimental Procedures

The experimental set-up is shown schematically in Fig. 1. The indentation was measured by a dial gage that permits reading up to 1/5000 in. The dial gage was mounted on a 'C' bracket fixed to the loading piston so that only the relative displacement between the indentor and the beam was recorded. The load applied pneumatically was measured using a load cell and a strain indicator. Two steel balls of diameters 6.35 mm (0.25") and 12.7 mm (0.5") were used as indentors. In all tests the beam was clamped at both ends.

Two types of laminated composites have been tested, namely glass/epoxy and graphite/epoxy. The glass/epoxy was Scotch Ply 1002 by the 3M Company. It contained 10 0°-plies and 9 90°-plies which alternate in the layup with one 0°-ply on top and on at the bottom. The thickness of the beam was 4.83 mm (0.19") and the width 38.1 mm (1.5"). The graphite/epoxy specimens were $[0/45/0/-45/0]_{2s}$ laminates. The thickness was 2.54 mm (0.1 in.). Two specimen widths were considered, namely 25.4 mm (1.0 in.) and 38.1 mm (1.5 in.). Their material properties are given as follows:

Glass/Epoxy:

$$E_1 = 39.3 \text{GPa} (5.7 \times 10^6 \text{ psi})$$
 $E_2 = 8.27 \text{GPa} (1.2 \times 10^6 \text{ psi})$
 $G_{12} = 4.14 \text{GPa} (0.6 \times 10^6 \text{ psi})$
 $V_{12} = 0.26$
(6)

Graphite/Epoxy:

$$E_1 = 120.7\text{GPa} (17.5 \times 10^6 \text{ psi})$$
 $E_2 = 7.93\text{GPa} (1.15 \times 10^6 \text{ psi})$
 $G_{12} = 5.52\text{GPa} (0.80 \times 10^6 \text{ psi})$
 $v_{12} = 0.30$
(7)

where subscripts 1 and 2 indicate directions parallel and perpendicular to the fiber, respectively.

Data were recorded in steps of about 2 to 5 units in the dial gage. Readings on the dial gage and strain indicator were taken about 10 to 20 seconds after the load was increased by one step.

- 4 Experimental Results and Modeling
- 4.1 Loading Curve

(A) Glass/Epoxy

For the glass/epoxy laminate, three sets of loading data were obtained for each span with a 6.35mm (0.25") diameter indentor. These data were used to determine the best fit for the power law, equation (4), using the least square method. A typical set of the data is presented in Fig. 2. The power indexes

for all three cases appear to be rather close to that of the classical Hertzian law for isotropic solids, i.e., n = 1.5. For this reason, we set n = 1.5, and then determined the contact coefficient k by using the least square fit. One of the resulting curves is shown in Fig. 3. The curves seem to fit the data very well also.

Table 1 summarizes the indentation law (the loading portion) obtained from the experimental data for the glass/epoxy laminate. It is interesting to note that with n=1.5, the values of k for different spans are almost a constant. This may be taken as an indication that the indentation law is independent of span. In other words, the bending stress in the range of these experiments does not influence the contact rigidity.

In Table 1, the modified Hertzian law, equation (3), is also presented using the material constants given in equation (6). It is found that the value of k is higher than the experimental values. However, it does provide a good estimate of the contact behavior.

(B) Graphite/Epoxy

For the 6.35 mm (0.25") diameter indentor, three sets of data were obtained for each span, while for the 12.7 mm (0.5") diameter indentor, except for one case, two sets of data were collected. The value of n was set equal to 1.5. The values of k fitted using each set of unloading data and all three (or two) sets of data are presented in Table 2. The corresponding modified Hertzian law are also shown in Table 2 for comparison. In Figs. 4-7 four typical sets of the experimental data are compared with the loading curves predicted by the power law.

From the values of k for the two indentors, it was found that k for 12.7 mm (0.5") indentor is about 1.8 times larger than that for the 6.35 mm (0.25") indentor. According to the Hertzian law, k is proportional to the square root of the diameter of the indentor and the increase in the k value should be 1.414.

From the experimental results, it is difficult to assess the effect of the specimen width. However, the variation in k for the 12.7 mm (0.5") indentor with respect to span and width seem to be smaller than that for the 6.37 mm (0.25") indentor.

4.2 Unloading Curve

(A) Glass/Epoxy

From the test results we observed that permanent deformation occurred after an indentation test at very low load levels. The unloading paths were very different from the loading path as can be seen from Fig. 8. The unloading curves were modeled by using equation (5) in which q and α_0 were determined from experimental data. Since the permanent indentation α_0 was difficult to measure, the whole set of data for each unloading was taken to determine q and α_0 by the least square method. The results showed that the values of q thus obtained varied between 2.0 and 3.0. It was found that q increased as the loading level increased. For q = 3.0 and q = 2.5, equation (5) seems to fit the overall data quite well as shown by Figs. 8-9. However, if q = 3.0, the value of α_0 might become negative in some cases. For this reason, q = 2.5 was chosen.

It should be pointed out that the value of α_0 obtained in this manner may not be the true permanent indentation. It is a value which can make

the power law given by equation (5) fit the total data in an unloading path.

Since α_0 depends on where the unloading begins, it seems that many unloading tests have to be performed in order that the unloading law given by equation (5) can be useful. In other words, the relation between α_0 and F_m must be established.

Setting q = 2.5, we rewrite equation (5) in the following form

$$F = s \left(\alpha - \alpha_0\right)^{5/2} \tag{8}$$

where

$$s = F_{\rm m}/(\alpha_{\rm m} - \alpha_{\rm o})^{5/2} \tag{9}$$

is an unloading rigidity. A fitting of the data can be obtained by fixing the value of s in all the unloading paths for finding α_0 . In doing so, we imply that the unloading rigidity s remains unchanged. Such assumption will greatly simplify the modeling of unloading. With this in mind, it is assumed that

$$k/s = \alpha_{Cr} \tag{10}$$

is a constant for a given material system and size of the indentor.

From the loading curve we have

$$F_{\rm m} = k \alpha_{\rm m}^{3/2} \tag{11}$$

By combining equations (9) through (11) the following equation is obtained

$$\alpha_0/\alpha_m = 1 - (\alpha_{cr}/\alpha_m)^{2/5} \tag{12}$$

This equation can be used to calculate α_0 as a function of α_m . From equation (12) it is easy to see that

$$\alpha_0 \ge 0$$
 as $\alpha_m \ge \alpha_{cr}$ (13)

i.e., when indentation passes the value $\alpha_{\mbox{cr}}$ then permanent deformation occurs. To avoid results which are not physically meaningful, we set

$$\alpha_0 = 0$$
 if $\alpha_m \leq \alpha_{cr}$

Hence, according to this model, $\alpha_{\mbox{cr}}$ can be regarded as the 'yield' point in indentation.

Since the energy dissipation in each loading-unloading cycle is of the main interest in this study, it is sensible to select α_0 in the unloading law so that the area under the unloading curve is equal to that calculated from the experimental data. One set of the unloading curves predicted by using the unloading law with this "area fit" is presented in Fig. 10. If these values of α_0 are substituted into equation (9), a range of value for s is obtained. By using the averaged value for s, the value for $\alpha_{\rm cr}$ is obtained from equation (10) as following

$$\alpha_{\rm cr} = 10.16 \times 10^{-2} \, \text{mm} \, (4.0 \times 10^{-3} \, \text{inch})$$
 (14)

The corresponding α_0 can then be obtained from equation (12). The unloading curves corresponding to those shown in Fig. 10 using this $\alpha_{\rm cr}$ are shown in Fig. 11. These curves seem to yield good agreement with experimental data. It was noted that a small variation in $\alpha_{\rm cr}$ would not have any appreciable effect on the unloading curve.

Table 3 summarizes the comparison of the areas under the unloading curves predicted by the direct area fit and the use of $\alpha_{\rm cr}$. The values of $\alpha_{\rm 0}$ obtained from the two approaches are also listed for comparison. The approach using $\alpha_{\rm cr}$ is found to be adequate in estimating the area under the unloading curve.

(B) Graphite/Epoxy

For the graphite/epoxy laminate, again q = 2.5 was used for the unloading law. Figs. 12-13 show some of the experimental data and the predicted unloading curves using values of α_0 obtained by matching the area under the unloading curve.

The best value of $\alpha_{\mbox{cr}}$ for graphite/epoxy was found to be

$$\alpha_{\rm cr} = 8.03 \times 10^{-2} \, \text{mm} \, (3.16 \times 10^{-3} \, \text{inch})$$
 (15)

for both sizes of indentor. The unloading curves predicted by using this $\alpha_{\rm Cr}$ value corresponding to the cases presented in Figs. 12-13 are presented in Figs. 14-15. Excellent agreement with experimental results was noted. The results for the 6.25 mm(0.25") and 12.7 mm(0.5") indentors obtained according to the above two approaches are summarized in Table 4 and Table 5, respectively. Note that the loading curves in Figs. 12-15 were plotted using a particular set of loading data for each case rather than the average value.

The fact that $\alpha_{\rm Cr}$ is not dependent on the indentor size is interesting. This may imply that $\alpha_{\rm Cr}$ is a material property similar to the yield stress for mild steel.

4.3 Reloading Curve

In the case where multiple impacts occur, the reloading behavior must be modeled. The reloading experiment was performed only on the graphite/epoxy laminate with the 1.27 cm (0.5") diameter indentor.

The reloading law was assumed to be in the form

$$F = k_1 \left(\alpha - \alpha_0\right)^p \tag{16}$$

where k_1 is a reloading rigidity. From the experimental data, p = 1.5 seemed to have fitted the data best.

It was observed that when the loading level was not too high, then the reloading curve always returned to where the unloading began. If such condition is imposed on the reloading law given by equation (16), then we have

$$k_1 = F_{\rm m}/(\alpha_{\rm m} - \alpha_{\rm o})^{3/2} \tag{17}$$

Thus the reloading rigidity k_1 is determined if the unloading condition $(F_m, \, \alpha_m, \, \text{and} \, \alpha_0)$ is specified. In other words, there is no need to perform reloading experiments to find the reloading rigidity k_1 .

Figs. 16-17 show typical experimental data and the predicted reloading curves obtained according to equations (16-17). Good agreement is noted.

Table 6 shows a number of values of k_1 computed according to equation (17). It is seen that these values are quite close to the loading rigidity k for small α_0 . However, for higher loading levels, a substantial deviation exists between these two values.

5 Discussion

From the results for the graphite/epoxy laminate, some scatter in the value of k in the loading law is noted even when the same material properties, indentor, and loading condition are used. This could be attributed to local material nonhomogeneity in the composite.

Being accustomed to the use of stress-strain relation to describe solid material properties one would attempt to modify the loading law into a similar form. A natural step that one would take is to divide the contact force F by a reference area and the indentation α by a reference length. Using the projection of the contact area, $2\pi D_{\rm S} \alpha$, as the reference area and the critical indentation $\alpha_{\rm Cr}$ as the reference length, we obtain from the indentation law the following

$$F/(\pi D_s \alpha) = \left[k \alpha_{cr}^{1/2}/(\pi D_s)\right](\alpha/\alpha_{cr})^{1/2}$$
(18)

Such form does not offer any advantage over the original form.

If the reference area $\pi D_s \alpha_{cr}$, the projection of the contact area when $\alpha = \alpha_{cr}$, is used instead, then the indentation law can be modified into

$$F' = k' (\alpha')^{3/2}$$
 (19)

where

$$F' = F/(D_{S}^{\alpha}cr)$$
 (20)

$$k' = k \alpha_{\rm cr}^{1/2}/D_{\rm s} \tag{21}$$

$$\alpha^{1} = \alpha/\alpha_{\rm cr}$$
 (22)

Note that F' has the unit of stress. Values of k' for the graphite/epoxy laminate are summarized in Table 7.

From equation (21), it is evident that k' becomes a constant if k is proportional to the diameter of the indentor. From our experimental data for the two indentor sizes, it appears that k is proportional to $(D_s)^{0.85}$ as opposed to $(D_s)^{0.5}$ predicted by the classical Hertzian law. More experimental data from more indentor sizes are needed to establish the relationship between k and the size of indentor.

In summary, we have established loading, unloading and reloading laws for glass/epoxy and graphite/epoxy laminates in contact with steel balls. For loading and reloading, 1.5 power laws seem to fit the data and for unloading, 2.5 power seems adequate. By using the critical indentation, $\alpha_{\rm cr}$, permanent indentations $\alpha_{\rm o}$ can be related to the unloading force $F_{\rm m}$, and consequently only one unloading curve has to be established experimentally. Further, since $\alpha_{\rm cr}$ seems to depend only on the material properties, only one unloading test needs to be conducted for each material system. For reloading, if equation (16) is employed, no unloading tests are needed to establish the unloading law.

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Table 1-Loading law F=k α^n for glass/epoxy with 6.35 mm diameter indentor, F in N and α in mm (F in 1b and α in inch).

	Glass/Epoxy:[(0	/90) ₄ /0/90/0	/(90/0) ₄]	
Span, mm	(in.)	50.8 (2.0)	101.6 (4.0)	152.4(6.0)
Least Squares Fit	n k, N/mm ⁿ (lb./in ⁿ)	1.70 x 10 ⁴	1.54 1.71 x 10 ⁴ (5.60x10 ⁵)	
1.5 Power Fit	n k, N/mm ^{1.5} (1b/in. ^{1.5})		1.5 1.61 × 10 ⁴ (4.63×10 ⁵)	
Modified Hertzian Law, Eq. (3)	$F = 1.90 \times 10$ $(F = 5.46 \times 1)$ $E_S = 207 \text{ GPa}$ $E_2 = 8.27 \text{ GPa}$	$0^5 _{\alpha}^{1.5}$, F (30 x 10^6 p	in 1b, α in s si), ν _s = 0.3	3

Table 2-Loading law F= $k_{\alpha}^{1.5}$ for $[0/45/0/-45/0]_{2s}$ graphite/epoxy; F in N and α in mm (F in 1b and α in inch).

Ball Dia., mm (in.)		6.35 (0.25)	0.25)		·	12.7 (0.50)	0)	
Span, mm (in.)	50.8 (2.0)	0)	101.6 (4.0)	(4.0)	50.8 (2.0)	0)	101.6 (4.0)	(4.0)
Width, mm (in.)	25.4(1.0)	25.4(1.0) 38.1(1.5)	25.4(1.0)	25.4(1.0) 38.1(1.5)	25.4(1.0)	38.1(1.5)	38.1(1.5) 25.4(1.0) 38.1(1.5)	38.1(1.5)
	2.00	1.82	1.78	2.14	3.30	3.36	3.33	3.68
×.	(5.77)	(5.23)	(5.14)	(6.17)	(9.51)	(6.67)	(6.59)	(10.59)
10 ⁴ N/mm ^{1.5} ,	2.13	1.83	1.82	2.20	3.59	3.31	3.18	3.48
(10 ⁵ 1b/in. ^{1.5})	(6.13)	(5.27)	(5.23)	(6.34)	(10.33)	(6.53)	(6.15)	(10.01)
	2.06	1.85	1.83	2.32	3.56			
	(5.92)	(5.33)	(5.28)	(6.68)	(10.24)			
k, Group Fit	2.06	1.85	1.81	2.19	3.47	3.34	3.23	3.60
10 ⁴ N/mm ^{1.5} (10 ⁵ 1b/in. ^{1.5})	(5.94)	(5.33)	(5.22)	(6.29)	(86.6)	(3.62)	(6.30)	(10.37)
Modified	$F = 1.82 \times 10^4 \text{ a}^{1.5}$	104 al.5			F = 2.5	$F = 2.57 \times 10^4 a^{1.5}$	5.	
Hertzian	(F = 5.24)	$(F = 5.24 \times 10^5 a^{1.5})$	·		(F = 7.	$(F = 7.41 \times 10^5 \text{g}^{1.5})$	(-5)	
Law, Eq.(3)	$E_S = 207 G$	Pa (30 x 10	ο psi), ν _s	$= 0.3, E_2$	207 GPa (30 x 10^{6} psi), $v_{s} = 0.3$, $E_{z} = 7.93$ GPa (1.15 x 10^{6} psi)	(1.15 × 10 ⁶	psi)	

Table 3-Values of α_{0} and area under the unloading curve by different fits for glass/enoxy

(in			EO 8 (2 0)	100			101 6 (4 0)	(0)			152 4 (6.0)	(
Spatt, IIII. / III. / K. N/mm ^{1.5} (16/in 1.5)	/in 1.5,	1,60	× 10 ⁴ (1.60 × 10 ⁴ (4.62 × 10 ⁵)	05)	1.61	104 (4.	1.61 × 10 ⁴ (4.63 × 10 ⁵)		1.60	× 10 ⁴ (4	$1.60 \times 10^4 (4.59 \times 10^5)$	5)
F _m , N		529	842	1513	2206	460	1362	1964	3104	518	1016	1594	2037
(16)		(119)	(189)	(340)	(496)	(103)	(306)	(445)	(869)	(116)	(822)	(358)	(458)
α _m , 10 ⁻² mm	- Ha	10.3	14.0	20.7	26.6	9.40	19.3	24.6	30.1	10.2	16.0	21.5	25.3
(10 ⁻³ in.)	in.)	(4.05) (5.52)	(5.52)	(8.16)	(10.5)	(3.69)	(2.26)	(69.6)	(11.9)	(4.01)	(6.28)	(8.48)	(86.6)
	Area	1.24	3.38	4.27	7.70	0.30	3.12	6.71	9.42	1.17	2.49	6.53	8.69
α_0 , 10^{-2} mm	Fit	(0.49) (1.33)	(1.33)	(1.68)	(3.03)	(0.12)	(1.23)	(5.64)	(3.71)	(0.46)	(0.98)	(2.57)	(3.42)
(10 ⁻³ in.)	αcr	0.56	1.70	5.13	8.53	0.0	4.37	7.34	10.6	0.0	2.64	5.59	7.77
	Fit	(0.22) (0.67)	(0.67)	(2.02)	(3.36)	(0.0)	(1.72)	(5.89)	(4.18)	(0.0)	(1.04)	(2.20)	(3.06
Area,	Area	137	256	712	1194	119	829	1016	1570	133	390	683	970
10-2 mm-N	Fit	(121)	(227)	(630)	(1057)	(105)	(999)	(890)	(1390)	(118)	(346)	(605)	(828)
(10 ⁻⁴ in1b)	acr	155	967	. \$29	1142	123	581	696	1481	150	387	726	1024
	Fit	(137)	(292)	(296)	(1011) (109)		(514)	(858)	(11311)	(133)	(342)	(643)	(906)

Table 4-Values of α_0 and area under unloading curve by different fits for graphite/epoxy with 0 6.35 mm (0.25 in.) indentor

					-								
Span, mm (in.)				50.8 (2.0)	(0.5					101.6 (4.0)	6		
Width, mm (in.)	7	25.	25.4 (1.0)		38.1	38.1 (1.5)		25.4	25.4 (1.0)		.38.	38.1 (1.5)	
k. N/mm ^{1.5} (1b/in. ¹	5/in. 1.5)		2.06×10 ⁴ (5.92×10 ⁵)	105)	1.85×10	1.85×10 ⁴ (5.33 × 10 ⁵)	102)	$1.83 \times 10^4 \ (5.28 \times 10^5)$	4 (5.28	× 10 ⁵)	2.32×10	$2.32 \times 10^4 \ (6.68 \times 10^5)$	× 10 ⁵)
N		899	934	1223	273	199		408	612	844	277	299	1210
(15)	_	(150)	(210)	(275)	(61.3) (126)	1	(224)	(21.7)	(138)	(190)	(62.3) (149)	(149)	(272)
α, 10 ⁻² mm		10.2	12.7	15.2	00.9	9.70	14.2	7.90	10.4	12.9	5.20	9.30	14.0
(10 ⁻³ in.)	. ((4.01)	(5.01)	(00.9)	(2.37)	(3.83)	(5.61)	(3.12)	(4.08) (5.06)	(2.06)	(2.06) (3.68)	(3.68)	(2.50)
~ 10 ⁻² mm	Area	0.94	1.80	2.79	0.05	0.43	2.13	00.0	0.41	1.55	0.00	0.61	1.85
	Fit	(0.37)	(0.71)	(1.10)	(0.05)	(0.17)	(0.84)	(00.0)	(0.16) (0.61)	(0.61)	(0.00) (0.24)	(0.24)	(0.73)
(10 ⁻³ in.)	8	0.91	2.13	3.45	0.00	0.71	2.92	0.00	1.02	2.21	00.0	0.56	2.77
	Fig. cr	(0.36)	(0.84)		(1.36) (0.00) (0.28)		(1.15)	(00.0)	(0.40) (0.87)	(0.87)	(0.00)	(0.22)	(1.09
Area	Area	188	291	435	46.5	149	345	92.2	174	272	41.4	165	418
10 ⁻² mm - N	Fit	(166)	(258)	(382)	(41.2)	(132)	(302)	(81.6)	(154) (241)	(241)	(36.7) (146)	(146)	(370)
	1	177	282	412	46.9	144	323	92.2	164	257	41.4	991	387
	Fit.	(156)	(220)	(392)	(41.5) (128)		(582)	(286) (81.6)	(145) (227)	(227)	(36.7) (147)	(147)	(342)

Table 5-Values of α and area under unloading curve by different fits for graphite/epoxy with 12.7 mm (0.5 in.) indentor

								-					
Span, mm (in.)	(]			50.8 (2.0)	(2.0)					101	101.6 (4.0)		
Width, mm (in.)	n.)	2	25.4 (1.0))	38.1 (1.5)	(1.5)		25.	25.4 (1.0)		38.	38.1 (1.5)	
k, N/mm ^{1.5} (1b/in. ^{1.5})	in. ^{1.5})	3.56x1	3.56×10 ⁴ (10.24×10 ⁵)	4×10 ⁵)	3.31×1	$3.31 \times 10^4 (9.53 \times 10^5)$	10 ²)	3.18×10	$3.18 \times 10^4 (9.15 \times 10^5)$	0 ₅)	3.60×1	$3.60 \times 10^{4} (10.37 \times 10^{5})$	к10 ⁵)
, m	Z	425	955	1479	61.2	1320	1645	227	791	1239	267	006	1285
	(1 _b)	(95.5)	(215)	(333)	(162)	(573)	(370)	(15)	(178)	(279)	(60.1)	(202)	(583)
α _m , 10	10-2 mm	5.10	00.6	12.0	7.80	11.7	13.5	3.70	8.50	1.15	3.80	8.60	10.8
(10 ⁻³ in) .	in) .	(2.01)	(3.53)	(4.73)	(3.07)	(4.60)	(5:32)	(1.46)	(3.35) (4.53)	(4.53)	(1.50)	(3.37)	(4.27)
α _ο , 10 ⁻² mm	Area	0.00	0.76	2.18	0.03	1.30	2.31	0.05	0.56	1.65	0.00	0.03	1.35
	Fit	(0.00)	(0.30)	(0.86)	(0.01)	(0.51)	(0.91)	(0.05)	(0.22) (0.65)	(0.65)	(0.00)	(0.01)	(0.53)
(10^{-3} in)	င်	0.00	0.38	1.78	00.00	1.68	2.51	00.00	0.20	1.55	00.0	0.20	1.22
	Fit	(0.00)	(0.15)	(0.70)	(00.00)	(0.66)	(0.99)	(0.00)	(0.08) (0.61)	(0.61)	(00.0)	(0.08)	(0.48)
Area,	Area	63.4	224	415	159	392	527	23.7	180	349	29.0	220	348
	Fit	(56.1)	(198)	(367)	(141)	(347)	(466)	(50.9)	(159)	(308)	(25.7)	(194)	(308)
10 ⁻² mm - N	ູ້ວ	63.4	234	432	160	379	516	24.0	188	353	29.0	214	353
(10 ⁻⁴ in1b)	Fit	(56.1) (207)	(202)	(382) (142)	- 1	(335) (457)	(457)	(21.2)	(166) (312)	(312)	(25.7)	(190)	(312)

Table 6-Comparison of loading rigidity k and reloading rigidity k_{1} for graphite/epoxy with 12.7 mm (0.5 in.) indentor

Span, mm (in.)	50	50.8 (2.0)			101.6	101.6 (4.0)			
Width, mm (in.)	25.	25.4 (1.0)		-	25.4	25.4 (1.0)	38.	38.1 (1.5)	
k, N/mm ^{1.5} (1b /in. ^{1.5})	$3.56 \times 10^4 (10.24 \times 10^5)$	(10,24)	(201)	3.18x1	$3.18 \times 10^4 (9.15 \times 10^5)$,×10 ⁵)	3.60x	3.60×10 ⁴ (10.37×10 ⁵)	37×10 ⁵)
F _m , N (1b)	428 (95)	955 (215)	1479 (333)	227	791	1239	267	900	1285
α _m , 10 ⁻² mm	5.11	8,97	12.0	3.71	8.51	11.5	3.81	8.56	10.8
(10 ⁻³ in.)	(2.01)	(3.53)	(4.73)	(1.46)	(3.35)	(4,53)	(4.53) (1.5)	(3.37)	(4.27)
α_0 , 10^{-2} mm	0.0	0.76	2.18	0.05	95.0	1.65	0.0	0.25	1.35
(10 ⁻³ in.)	(0.0)	(0:30)	(0.30) (0.86) (0.02) (0.22)	(0.03)	(0.22)	(0.0) (0.0)	(0.0)	(0.01)	(0.53)
10 ⁴ N/mm ^{1.5}	3.68	4.06	4.80	3,24	3,53	4.01	3,59	3.61	3.67
^{^1} , (10 ⁵ lb/in. ^{1.5)}	(10.6)	(11.7)	(10.6) (11.7) (13.8) (9.33) (10.2)	(6,33)	(10.2)	(11.5)	(11.5) (10.3)	(10.4)	(10.4) (10.6)

Table 7-Values of k for graphite/epoxy (Equation (19)).

			-					
Ball Diameter mm (in.)		6.35	6.35 (0.25)			12.7 (0.50)	0.50)	
Span, mm (in.)	50.8	50.8 (2.0)	101.6	(4.0)	101.6 (4.0) 50.8 (2.0)		101.6 (4.0)	(4.0)
Width, mm	25.4 38.1	38.1	25.4 38.1 25.4	38.1	25.4	38.1 25.4		38.1
(in.)	(1.0)	(1.5)	(1.0) (1.5) (1.0) (1.5) (1.0) (1.5) (1.0) (1.5)	(1.5)	(1.0)	(1.5)	(1.0)	(1.5)
GPa 0.92 0.81 0.98 0.77 0.74 0.72 0.81 (1.05 ns.i) (1.34) (1.18) (1.17) (1.42) (1.12) (1.08) (1.05) (1.17)	0.92	0.81	0.92 0.81 0.81 0.98 0.77	0.98	0.77	0.74	0.74 0.72 (1.05)	0.81
2	\- - - -	(2)		, <u> </u>	,	,		

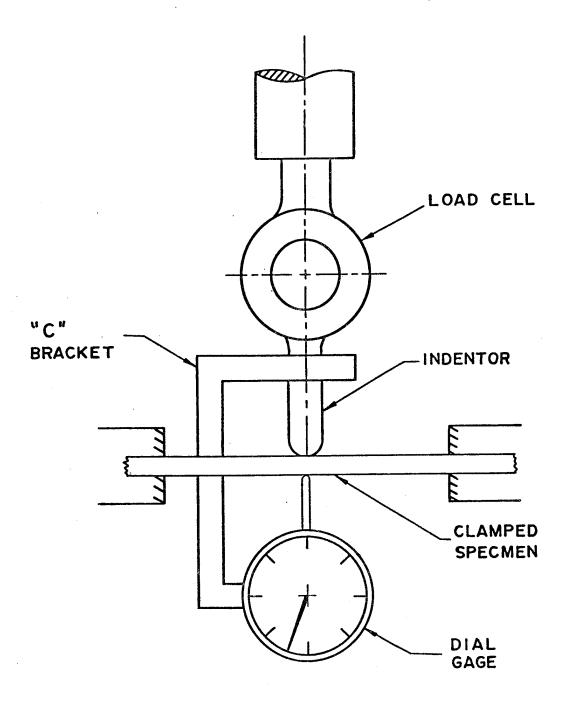


Fig. 1 Indentation test set-up

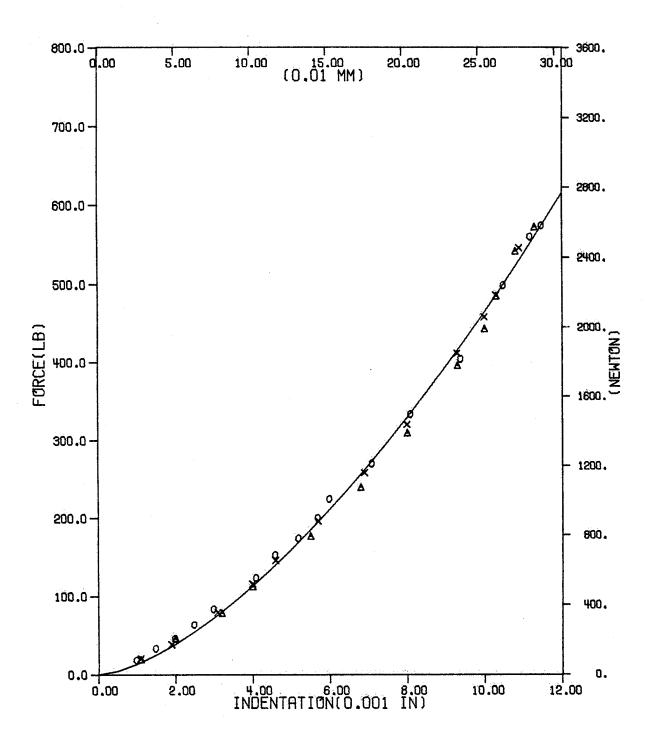


Fig. 2 - Least-square fit for loading for glass/epoxy with 50.8 mm(2")span and 6.35 mm (0.25") diameter indentor.

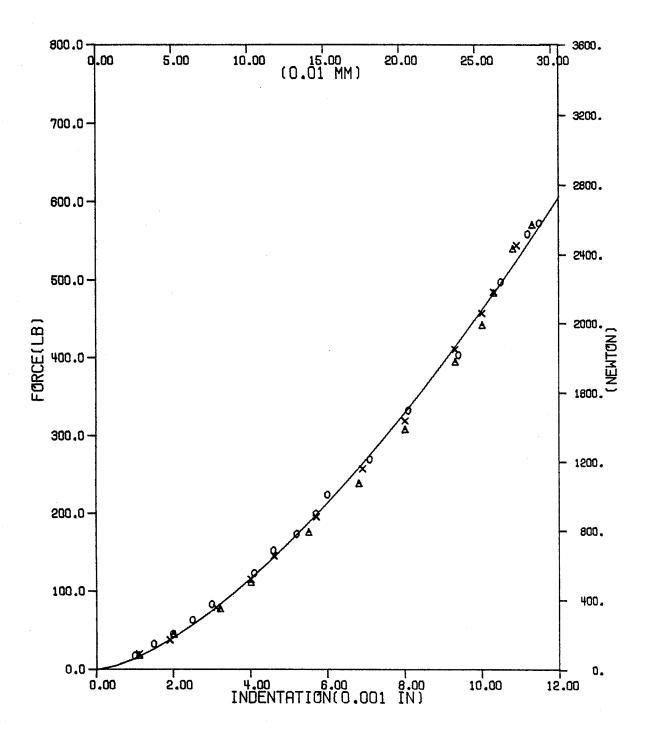


Fig. 3 - Least-square fit for loading with n = 1.5 for glass/epoxy with 50.8 mm(2")-span and 6.35 mm($\overline{0.25}$ ") diameter indentor.

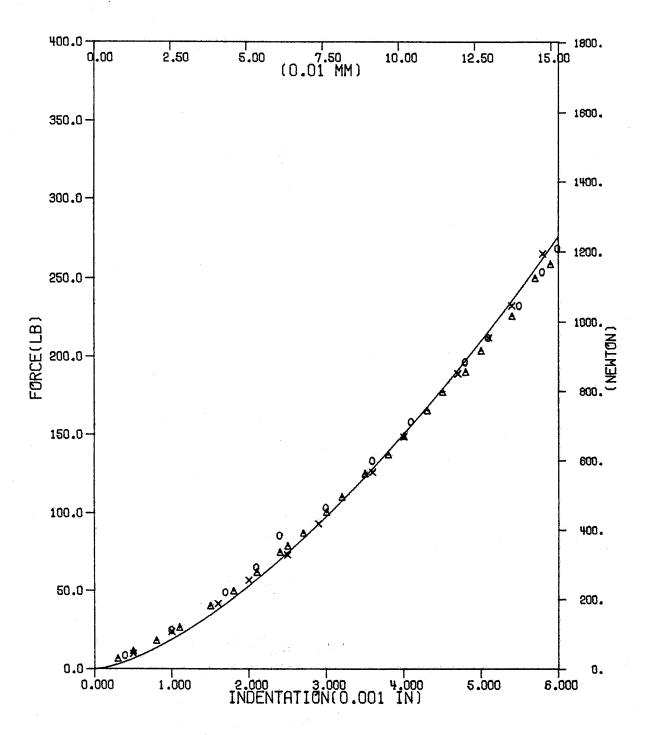


Fig. 4 - Least-square fit for loading with n = 1.5 for graphite/epoxy with 50.8 mm(2")-span 25.4 mm-width, and 6.35 mm (0.25") indentor.

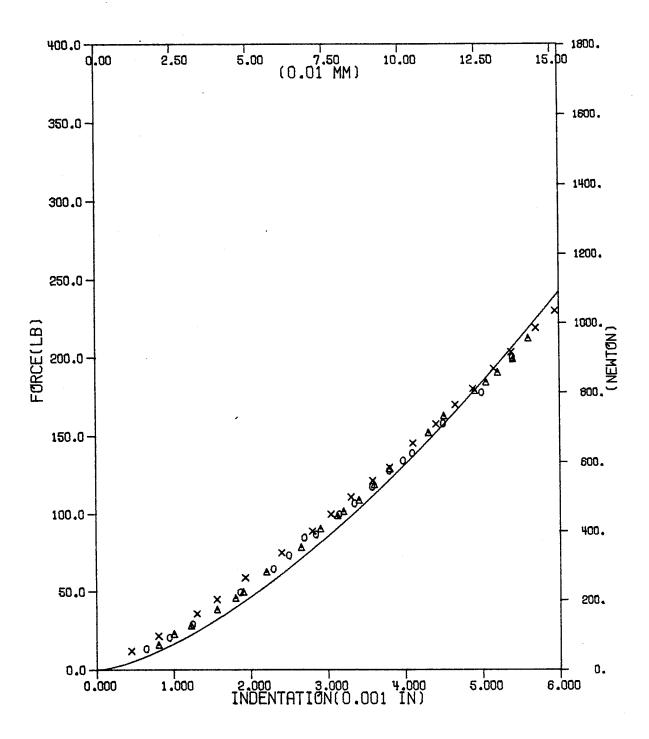


Fig. 5 - Least-square fit for loading with n = 1.5 for graphite/epoxy with 101.6 mm(4")-span, 25.4 mm-width, and 6.35 mm(0.25") indentor.

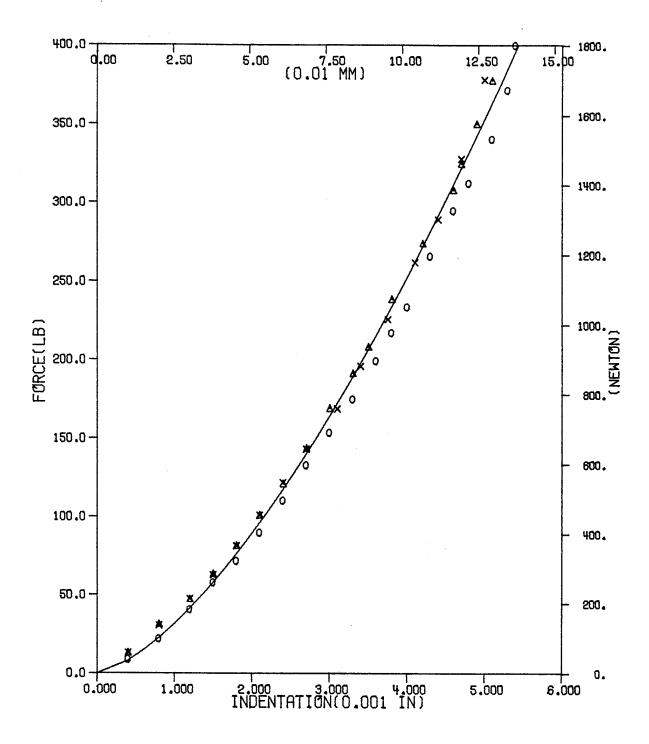


Fig. 6 - Least-square fit for loading with n = 1.5 for graphite/epoxy with 50.8 mm(2")-span, 25.4 mm(1")-width, and 12.7 mm(0.5") indentor.

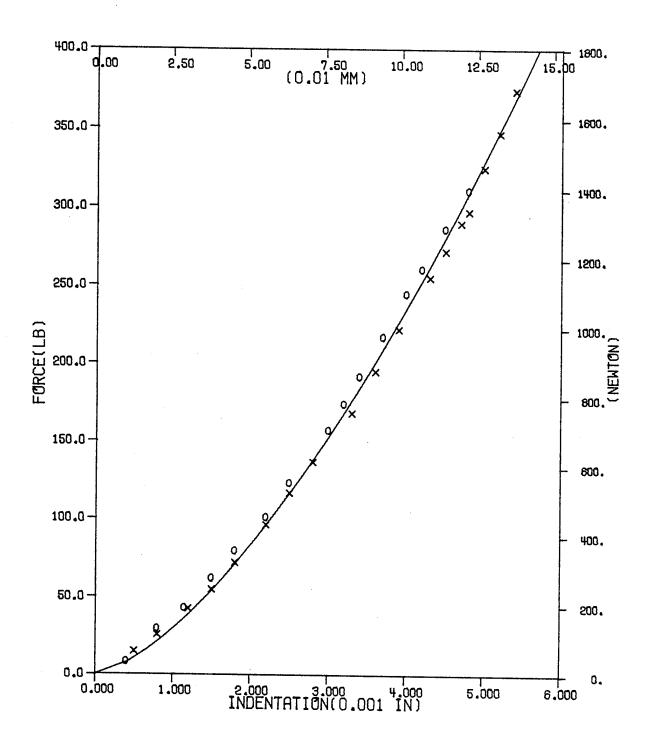


Fig. 7 - Least-square fit for loading with n = 1.5 for graphite/epoxy with 101.6 mm(4")-span, 25.4 mm(1")-width, and 12.7 mm(0.5") indentor.

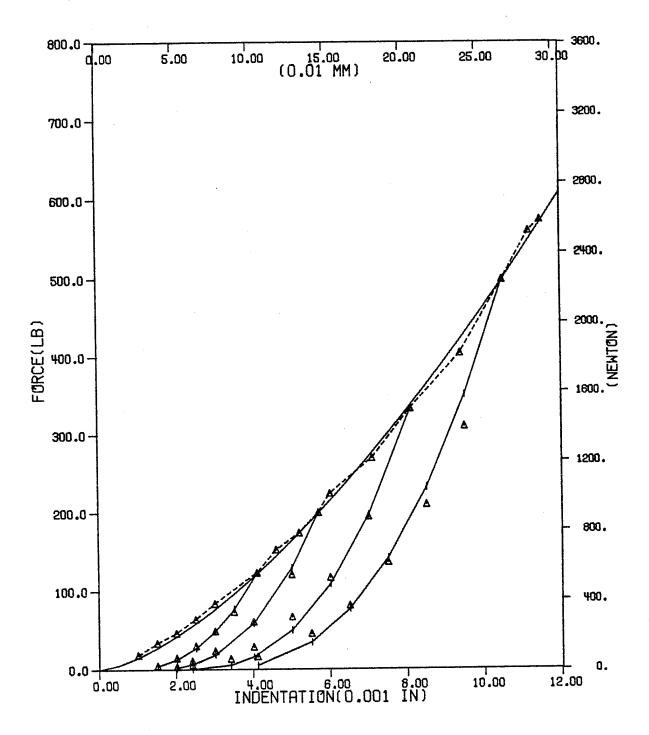


Fig. 8 - Unloading curves for glass/epoxy with q = 2.5, 50.8 mm(2")-span and 6.35 mm(0.25") indentor.

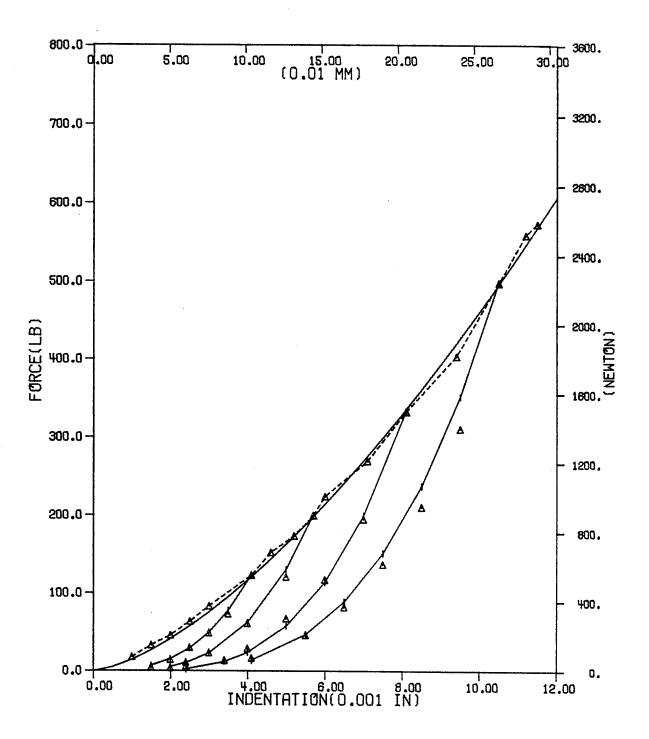


Fig. 9 - Unloading curves for glass/epoxy with q = 3.0, 50.8 mm(2")-span, and 6.35 mm(0.25") indentor.

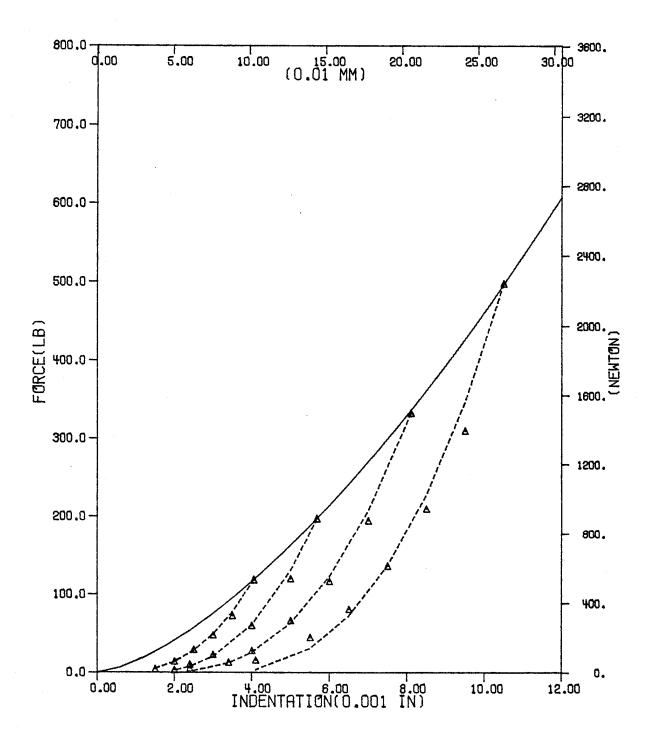


Fig. 10 - Unloading curves for glass/epoxy with 50.8 mm(2")-span and 6.35 mm(0.25) indentor using area fit.

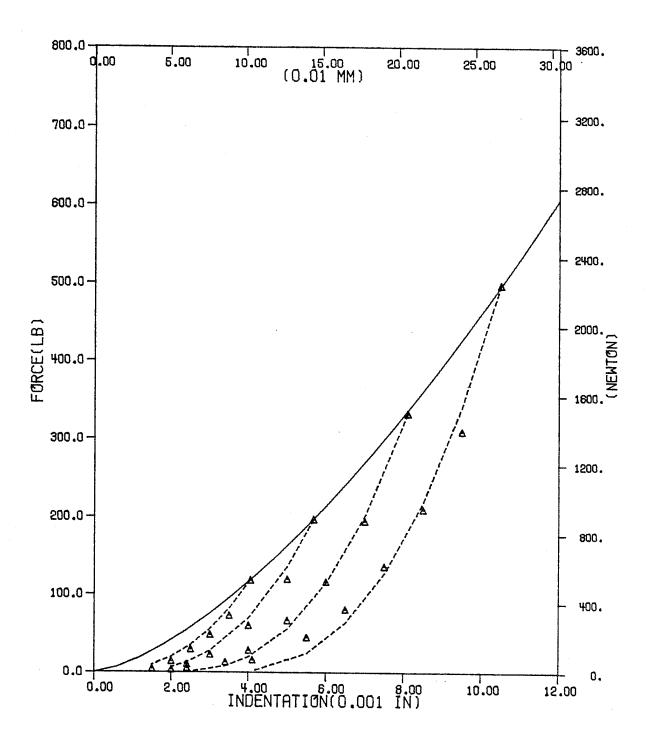


Fig. 11 - Unloading curves for glass/epoxy with 50.8 mm(2")-span and 6.35 mm(0.25") indentor using $\alpha_{\rm cr}$ = 0.102 mm(0.004").

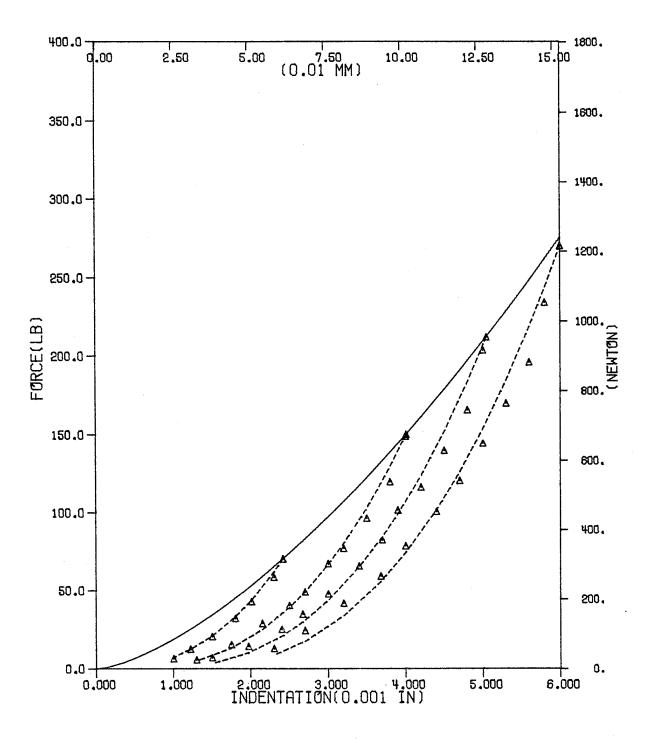


Fig. 12 - Unloading curves for graphite/epoxy with 50.8 mm(2")-span, 25.4 mm(1")-width and 6.35 mm(0.25") indentor using area fit.

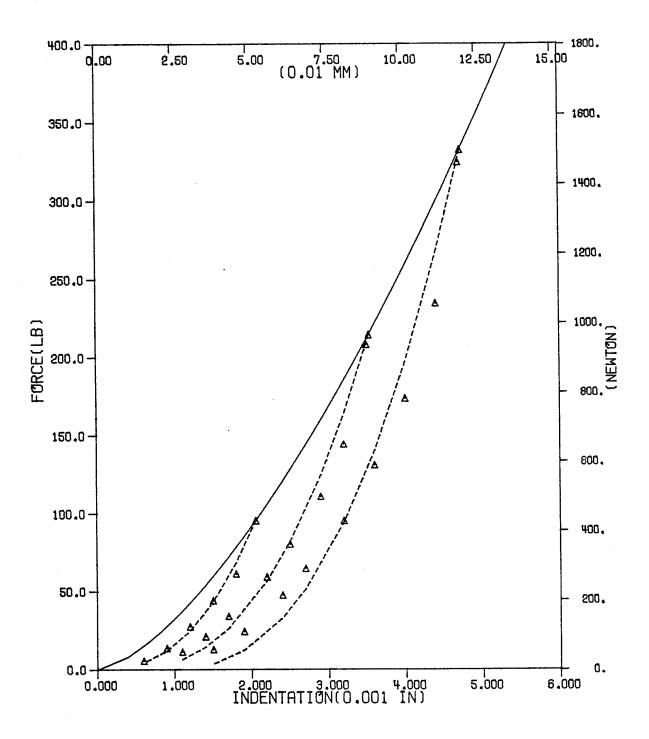


Fig. 13 - Unloading curves for graphite/epoxy with 50.8 mm(2")-span, 25.4 mm(1")-width, and 12.7 mm(0.5") indentor using area fit.

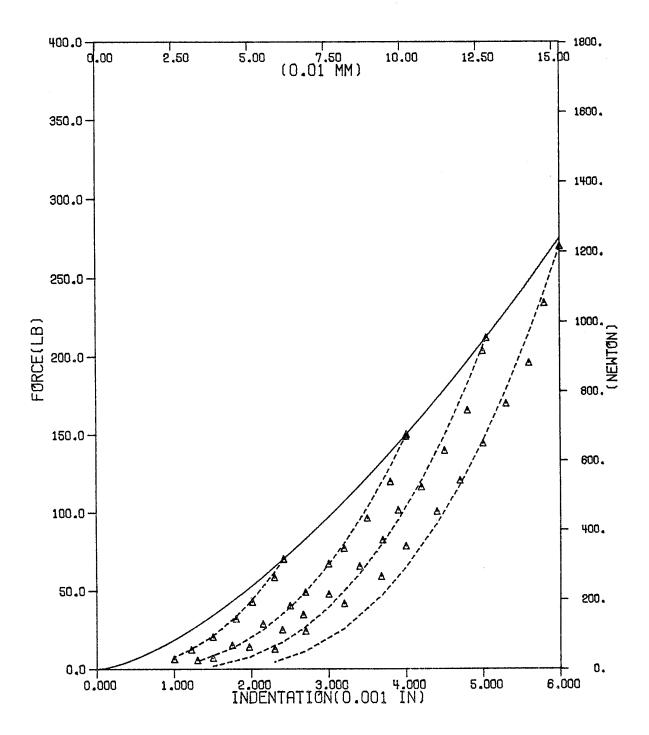


Fig. 14 - Unloading curves for graphite/epoxy with 50.8 mm(2")-span, 25. mm(1")-width, and 6.35 mm(0.25") indentor using α_{cr} = 0.0803 mm(0.00316").

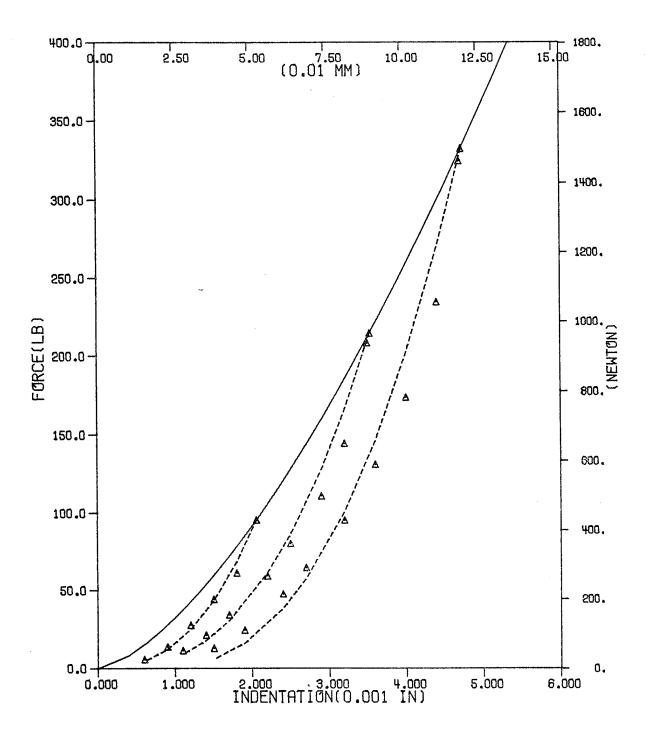


Fig. 15 - Unloading curves for graphite/epoxy with 50.8 mm(2")-span, 25.4 mm(1")-width, and 12.7 mm(0.5") indentor using $\alpha_{\rm Cr}$ = 0.0803 mm (0.00316").

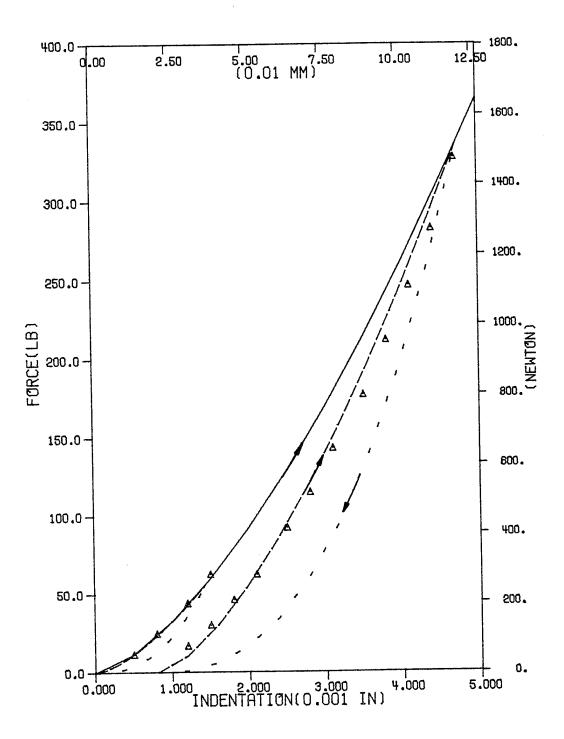


Fig. 16 - Reloading curves for graphite/epoxy with 50.8 mm(2")-span and 12.7 mm (0.5") indentor.

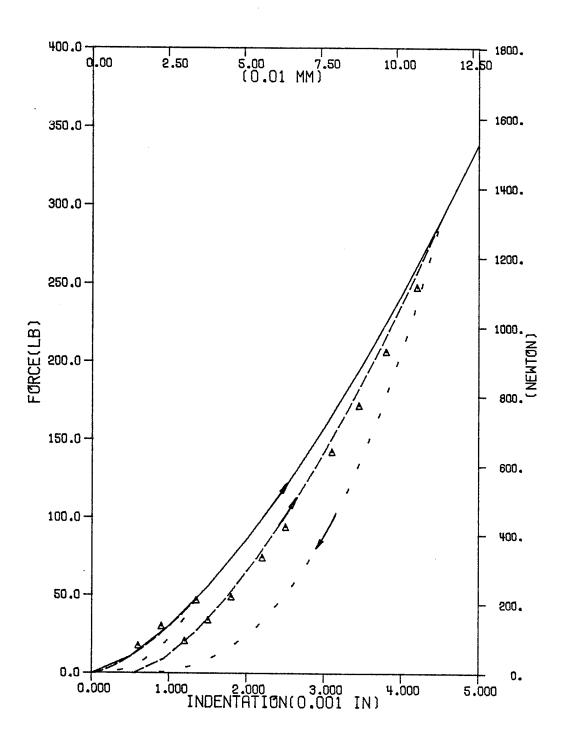


Fig. 17 - Reloading curves for graphite/epoxy with 101.6 mm(4")-span and 12.7 mm(0.5") indentor.

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